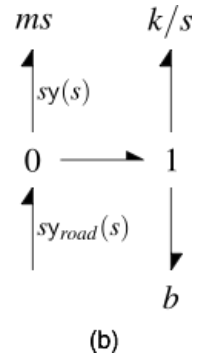
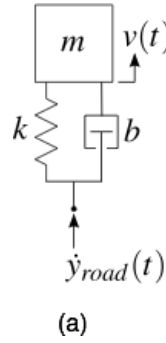


Chapter 8 Lecture Problems

Example 8.1

Find the steady-state response to a sinusoidal input displacement of the form  $y_{road} = (A \sin \omega t) \text{ m/s}$  where  $A=0.03 \text{ m}$  and  $\omega=10 \text{ rad/s}$ . The system parameters for  $m$ ,  $b$ , and  $k$  are  $500 \text{ kg}$ ,  $8000 \text{ N-s/m}$ , and  $34,000 \text{ N/m}$ , respectively. The transfer function is given below.

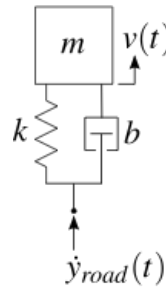
$$\frac{y(s)}{y_{road}(s)} = G(s) = \frac{bs + k}{ms^2 + bs + k}$$



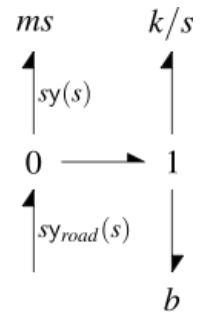
Chapter 8 Lecture Problems

Solve the previous problem using MATLAB. The transfer function and system diagram are given.

$$\frac{y(s)}{y_{road}(s)} = G(s) = \frac{bs + k}{ms^2 + bs + k}$$



(a)

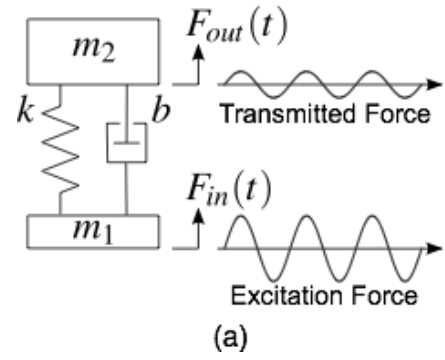


(b)

## Chapter 8 Lecture Problems

### Example 8.3

Find the transmissibility if the foundation is forced by an excitation  $F_{in}(t) = (5\sin 2t)N$ . The first mass, damping constant, spring stiffness, and second mass are 2 kg, 2 N-s/m, 5 N/m, and 1 kg, respectively.

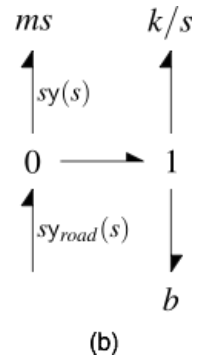
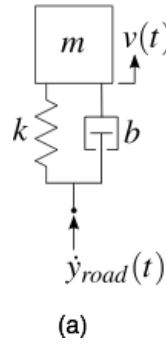


Chapter 8 Lecture Problems

Example 8.1: Motion Transmissibility

Determine the motion transmissibility from the system depicted in Example 8.1

$$\frac{y(s)}{y_{road}(s)} = G(s) = \frac{bs + k}{ms^2 + bs + k}$$

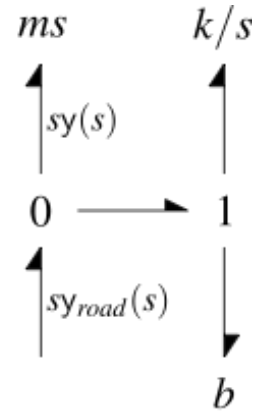
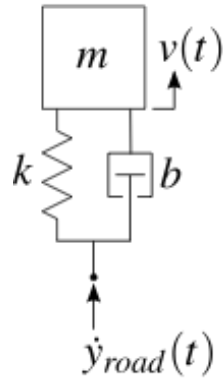


Chapter 8 Lecture Problems

The Quarter-Car Suspension

Rewrite the motion transmissibility in terms of the damping ratio and normalized frequency.

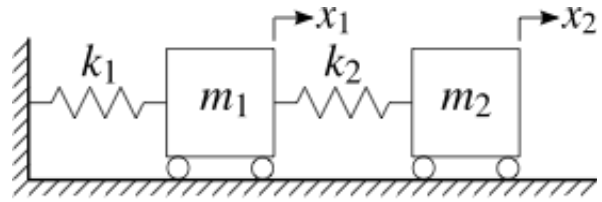
$$TR = \frac{\sqrt{k^2 + (b\omega)^2}}{\sqrt{(k - m\omega^2)^2 + (b\omega)^2}}$$



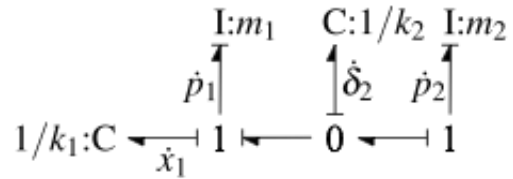
Chapter 8 Lecture Problems

Example 8.4

Find the natural frequencies of vibration and the respective mode shapes for the two DOF structure model and an axially vibrating beam where  $k_1 = 2k_2$  and  $m_1 = 2m_2$ . For simplicity,  $k_2 = k$  and  $m_2 = m$ .



(a)



(b)