WELCOME TO MECE 2301 STATICS!

Samantha Ramirez, MSE

Syllabus Information

Course Information

- TR 12:30 PM 1:45 PM
- PLTL: 2:00 PM 3:15 PM
- Pre-requisites:
 - "C" or better in PHYS 2425 and MECE 1101 and "C" or better or concurrent enrollment in MATH 2414
- Required Materials
 - Vector Mechanics for Engineers Statics & Dynamics, Beer, 12th ed, Connect Access with eText

Instructor Contact Information

- Office: EENGR 3.261
- Office Hours
 TR 10:00 AM 11:00 AM
- Email:
 - samantha.Ramirez@utrgv.edu
- Website:
 - https://faculty.utrgv.edu/samantha.ramirez

Course Structure

- Pre-Lecture (Due before class by 12:30 PM)
 - SmartBook assignment in MH Connect
 - Aimed to introduce topics before we cover them in class
- Lecture
 - 12:30 PM Course content and example problems
 - In-class quizzes on Tuesdays covering content from previous week
 - 2:00 PM Mandatory PLTL session
 - Session work due by 3:15 PM of same day
- Post-Lecture (Due by class time 12:30 PM)
 - Homework in MH Connect
 - Late submissions accepted until 11:59 PM with a 10% penalty.
 - No submissions accepted after 11:59 PM.

Grading Policy

- 3 Midterm Exams 45% (15% each)
 Scheduled on Fridays from 8:30 AM 10:30 AM in ESCNE 2.106 • Exam 1: 2/16/24, Exam 2: 3/22/24, Exam 3: 4/26/24
 - To take a midtern exam, you cannot have more than 2 unexcused absences from class at 12:15 PM and 2 unexcused absences from PLTL at 2:00 PM
 - Once a graded exam is returned, you only have 24 hours to contest your exam grade
- Quizzes 15% Every Tuesday

 - SmartBook assignments due at class time before content is covered
- Homework 10%
 McGraw-Hill Connect link in Blackboard
 - 10% penalty for late work accepted until 11:59 PM on due date
- PLTL 10%
 Attendance is 4%
 - Session Work is 6% and graded following rubric in syllabus
- Cumulative Final Exam 20%

Classroom Expectations

- Attendance is taken daily
- No live Zoom sessions
- Participation during class
 - Calculating answers, taking notes, etc.
- If you are going to miss class, email me before class detailing your situation. If you are sick, provide a doctor's excuse or test results (with name and DOB).
 - DO NOT WAIT UNTIL AFTER DUE DATES/EXAM DATES TO LET ME KNOW.

PRE-REQUISITE MATH

Pre-Requisite Math Topics

- Geometry
 - Pythagorean Theorem, areas, coordinate systems
- Trigonometry (Pre-Calculus)
 SOH-CAH-TOA

 - Law of Sine & Law of Cosine
- Algebra
 - System of Linear Equations
 - Roots of a Quadratic Equation
- Calculus
 - Integrals
 - Derivatives







Law of Sine & Law of Cosine

- Applies to all triangles
- Law of Sine is used when you know either:
 - 2 angles and 1 side
 - 2 sides and 1 angle

$$\frac{\sin\theta}{a} = \frac{\sin\alpha}{b} = \frac{\sin\beta}{c}$$

- Law of Cosine is used when you know either:
 - 3 sides
 - 2 sides and 1 angle

$$c^{2} = a^{2} + b^{2} - 2abcos(\beta)$$
$$a^{2} = c^{2} + b^{2} - 2cbcos(\theta)$$
$$b^{2} = a^{2} + c^{2} - 2cacos(\alpha)$$







- 1. What is θ if a=23 mm, b=50 mm, and c=48 mm?
- 2. What is c if a=67 in, λ =84°, and β =27°?



System of Linear Equations

- A collection of one or more equations with the same variables
 - The number of equations and the number of unknowns are the same
- 1. Rearrange equations so that variables are in the same order for all equations
- 2. For 2 equations/2 unknowns, you can use the graphing method, the substitution method, or the elimination method.
- 3. For 3 equations/3 unknowns, you can use the linear combination method.
 - a) Take 2 equations at a time to eliminate one variable. Then use the resulting equations with 2 variables to eliminate another variable.

Example 3

• Solve for a and b in the following equations using the substitution method and the elimination method.

7a - 6b = 1934 + 9a = 12b

Example 4

• Solve for x, y, and z for the following equation system:

$$9x - 6y + 7z = 62$$

 $6z - 7x = 87 - 3y$
 $56 + 8x = 2z - 9y$

• Solution in Blackboard

Roots of a Quadratic Equation

• Quadratic Formula

$$x = \frac{-b \pm \sqrt[2]{b^2 - 4ac}}{2a}$$

• Use the quadratic formula to solve for the roots (x) of a quadratic equation of the following form:

$$ax^2 + bx + c = 0$$

Example 5

• Find the roots of the following equations:

$$5x^2 + 23x - 67 = 0$$

$$23 - 45x + 2x^2 = 3x^2 - 10$$

Derivatives – Product Rule

• Product (Chain) Rule

$$\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$$

Example 6

• Find the derivative of 5xcos(x) and evaluate it at x=0.





• Find the integral of $\cos(x) + 4x^3$ from o to A.

• Find the integral of $16x^6 + \sin(x)$.

WHAT IS STATICS? & UNIT CONVERSIONS





Fundamental Concepts

- Length: used to locate the position of a point in space
- <u>Time</u>: the interval between two events and required with position to define an event
- <u>Mass</u>: the quantity of matter OR a measure of its inertia (resistance to a change in its motion)
- <u>Force</u>: the push or pull of one body on another which has a point of application, magnitude, and direction

Important Principles and Laws

- Newton's Three Laws
 - 1. If a particle is acted on by a balanced force system, it will continue with the same state of motion. The direction and magnitude of the motion will remain unchanged.
 - An object at rest will remain at rest unless acted upon by an unbalanced force.

•
$$\sum \vec{F} = \vec{0}$$

- 2. The resultant force acting on a particle of mass is proportional to the acceleration of the particle.
 - $\sum \vec{F} = m\vec{a}$
 - When the acceleration of a particle is o, Newton's second law becomes F = o which is the central focus of statics.
- 3. The forces of action and reaction between interacting bodies are equal in magnitude, opposite in direction, and collinear.
 - For every action, there is an equal and opposite reaction.



Important Principles and Laws

- Newton's Law of Gravitation
 - Two particles are attracted with equal and opposite forces

$$F = G \frac{m_1 m_2}{r^2}$$

- m_1 and m_2 are masses of two particles attracted to each other
- G is the constant of gravitation of 6.673x10⁻¹¹ m³/kgs²
- r is the distance between two particles
- What happens when one particle is Earth and the second particle is an object on Earth?

$$F = G \frac{m_1 m_2}{r^2} \to W = G \frac{m_e m}{r_e^2} = mg$$

https://mediao.giphy.com/media/lsJgz5SmyhtdybtaU/giphy.gif

g is Earth's gravitational constant 9.81 m/s² or 32.2 ft/s²

Units

SI Units

- International System of Units
- Used mostly around the world

US Customary Units

- Used in the US only
 - Imperial units are used in England now

Quantity	SI Units	US Customary Units
Time	S	S
Length	m	ft
Mass	kg	slug

Challenge

• Derive the units for weight in both unit systems.



Weight

• Newton's Second Law states:

$$F = ma$$

• The weight of an object of mass m on the surface of Earth is

$$W = mg$$

$$W = m(kg) \times 9.81 \frac{m}{s^2} \qquad W = m(slug) \times 32.2 \frac{ft}{s^2}$$

$$W\left(\frac{kgm}{s^2}\right) = m(kg) \times 9.81 \frac{m}{s^2} \qquad W\left(\frac{slugft}{s^2}\right) = m(slug) \times 32.2 \frac{ft}{s^2}$$

$$W(N) = m(kg) \times 9.81 \frac{m}{s^2} \qquad W(lb_f) = m(slug) \times 32.2 \frac{ft}{s^2}$$

Basic Units & Conversions

Quantity	SI Units	US Customary Units
Time	S	S
Length	m	ft
Mass	kg	slug
Force	Ν	lb

Quantity	Unit of Measurement	Equals	Unit of Measurement
Longth	1 in	=	0.0254 m
Length	1 mi	=	5280 ft
Mass	1 slug	=	14.594 kg
IVIdSS	ı lb _m	=	o.4536 kg
Force	1 lb	=	4.448 N

Unit Prefixes

Multiplication Factor	Prefix	Symbol
1 000 000 000	Giga	G
1 000 000	Mega	М
1000	Kilo	k
0.01	Centi*	с
0.001	Milli	m
0.000 0001	Micro	μ
0.000 000 001	Nano	n

Engineering Notation
A version of the scientific notation in which the exponent must be a multiple of 3

Units in Engineering

• If you work a problem and your units are incorrect, or

• If you work a problem and you don't indicate the units,

Your answer is WRONG!

Numerical Calculations

- Dimensional Homogeneity
 - Dimensions must be the same on both sides of the equal sign
- Significant Figures
 - Determines the accuracy of the number
 - Do not record more significant figures than necessary
 - Practical Rule
 - Use 4 figures to record numbers starting with a "1"
 - Use 3 figures in all other cases
- Rounding off numbers
 - Necessary so the accuracy of the result will be the same as that of the problem data
 - Be consistent with the textbook



Example 1

• Convert the velocity v=75 km/hr to units of mi/hr.


• Convert the mass m=350 slug to units of kg.

• Convert the torque T=76.8 Nm to units of lb-in.

- Calculate the weight in lb_f of 120 lb_m .

 \bullet Calculate the weight in $\rm lb_{f}$ of a body with a mass of 58 kg.

• Calculate the area of a lot in m² if it measures 1575 ft².

• Convert an acceleration of 9000 mi/h² to m/s².



STATICS OF PARTICLES



- Body: substance that occupies space and has a defined boundary
- <u>Space</u>: the geometric region in which the physical events of interest in mechanics occur
- <u>Scalar</u>: a quantity represented by magnitude alone • i.e. mass, temperature, pressure, time, length
- <u>Vector</u>: a quantity represented by both magnitude and direction
 i.e. velocity, acceleration, force, displacement (x)

Particle

- A body with negligible dimensions but not necessarily small with respect to you
- Earth is a particle when studying its motion around the sun





https://upload.wikimedia.org/wikipedia/commons/5/5f/Skycam_Husky_Stadium.jpg

https://www.insightsoninula.com/wpicontent/uprodus/2021/09/001-30ia1-39stent.jpg

Rigid Body

- A large number of particles occupying fixed positions with respect to one another
- A body which does not deform
- Nothing is completely rigid, but assuming so is continually used in the applications of mechanics









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https://mediao.giphy.com/media/lsJgz5SmyhtdybtaU/giphy.gif

g is Earth's gravitational constant 9.81 m/s² or 32.2 ft/s²



* of primary concern in Statics

FORCE SYSTEM

•Fx = Con

FG

•FM = FORCE OF MUSCLE ACTION •FY = ROTARY FORCE (TORQUE OR BIOMECHANICAL MOVEMENT)

le Insertion TAGE = FM / FG

•O = Angle of Muscle Ir

Introduction

- System of Forces Multiple forces treated as a group
 - If no external effect
 - Forces are "in balance"
 - Body is "in equilibrium"
 - Otherwise
 - Forces are "unbalanced"
 - And have a non-zero "resultant"
- Equivalent Force Systems • Produce the same external effect
 - Have the same "resultant"

- Resultant
- The simplest equivalent system to which the original system will reduce
- Reduction
 - The process of reducing a force system to a simpler equivalent system
- Resolution
 - The process of expanding a force or force system into a less simple equivalent sýstem
- Component of a Force
 - One of the two or more forces into which the given force may be resolvedoo

ADDITION OF PLANAR FORCES

Scalars vs Vectors

Scalars

- Completely described with a magnitude (number) only
- Follow the rules of elementary algebra
- Examples
 - Mass
 - Density
 - Length
 - Area



Vectors

- Described by a magnitude (number) <u>AND</u> a direction
 Orientation and sense
 - Orientation and sense
- Add according to Parallelogram Law or Triangle Rule
- Examples
 - Force
 - Moment
 - Acceleration
 - Velocity

Vector Types and Operations

• Principle of Transmissibility

 A rigid body will remain unchanged if a force acting at a given point is replaced by a force with the same magnitude and direction at another point on the line of action



- Free Vector
 - Has a specific magnitude, slope, and sense <u>BUT</u> its line of action does <u>not</u> pass through a unique point in space
- Sliding Vector
 - Has a specific magnitude, slope, and sense <u>AND</u> its line of action passes through a unique point in space
 - Can be anywhere along its line of action
- Fixed Vector
 - Has a specific magnitude, slope, and sense and its line of action passes through a unique point in space
 - Point of application is confined to a fixed point on its line of action











• Determine the resultant force using a) the parallelogram law and b) the triangle rule.







• A telephone cable is clamped at A to the pole AB. Knowing that the tension in the right-hand portion of the cable is T_2 =1000 lb, determine by trigonometry (a) the required tension T_1 in the left-hand portion if the resultant **R** of the forces exerted by the cable at is to be vertical, and (b) the corresponding magnitude of **R**.



ADDING FORCES BY COMPONENTS









• Determine the resultant force using Cartesian Vector form.





• Determine the resultant force using Cartesian Vector form.





• Cable AC has a tension of 40 lb. Determine the resultant of the cable and the two applied forces acting at point C on the short link.



• Determine the resultant of the forces shown and the angle the resultant makes with the x-axis.


CHALLENGE PROBLEM





• Determine the resultant vector in Cartesian Vector form for the component forces shown.



ADDING FORCES IN SPACE







• A force of 500 N forms angles of 60°, 45°, and 120°, respectively, with the x, y, and z axes. Find the components F_{xr} , F_{yr} , and F_z of the force and express the force in terms of unit vectors.

• A force has the components F_x=20 lb, F_y=-30 lb, and F_z=60 lb. Determine its magnitude F and the angles θ_x , θ_y , and θ_z it forms with the coordinate axes.



• A rectangular plate is supported by three cables as shown. Knowing that the tension in cable AD is 429 N, determine the components of the force exerted on the plate at D.



Adding Concurrent Forces in Space

• When adding concurrent vectors in space, add like components of vectors in Cartesian Vector form.

$$\vec{A} = A_x \hat{\imath} + A_y \hat{\jmath} + A_z \hat{k}$$

$$\vec{B} = B_x \hat{\imath} + B_y \hat{\jmath} + B_z \hat{k}$$

$$\vec{R} = (A_x + B_x)\hat{\imath} + (A_y + B_y)\hat{\jmath} + (A_z + B_z)\hat{k}$$

• To determine the resultant, take the square root of the sum of the squares of the components.

$$R = \sqrt{R_x^2 + R_y^2 + R_z^2}$$

• Use the cosine function to determine the direction angles of the resultant vector.

$$\cos\theta_x = \frac{R_x}{R}$$
 $\cos\theta_y = \frac{R_y}{R}$ $\cos\theta_z = \frac{R_z}{R}$

• Knowing that the tension is 425 lb in cable AB and 510 lb in AC, determine the magnitude and direction of the resultant of the forces exerted at A by the two cables.



PROJECTION OF A VECTOR



- If $\vec{A} = 20\hat{\imath} + 30\hat{\jmath} + 10\hat{k}$, $\vec{B} = 4\hat{\imath} + 6\hat{\jmath} 5\hat{k}$, and $\vec{C} = 7\hat{\imath} 15\hat{\jmath} + 12\hat{k}$, calculate the angle between the following vectors: \vec{A} and \vec{B}

 - \vec{C} and \vec{B}
 - \vec{A} and \vec{C}





- Knowing that the tension in cable AC is 280 lb, determine:
 - The angle between cable AC and the boom AB
 - The projection on AB of the force exerted by cable AC at point A



EQUILIBRIUM OF A PARTICLE

Equilibrium of a Particle

• When the resultant of all the forces acting on a particle is zero, the particle is in equilibrium.

$$\vec{R} = \Sigma \vec{F} = 0$$

• Scalar form for equilibrium of a particle

$$\Sigma F_{\chi} = 0$$
 $\Sigma F_{\gamma} = 0$

 If the resultant force acting on a particle is zero, the particle will remain at rest (if originally at rest) or will move with constant speed in a straight link (if originally in motion).



 $\Sigma F_z = 0$



- Space Diagram
 - A sketch showing the physical conditions of the problem
- Free-Body Diagram
 - A sketch showing a particle (or component) and all the forces acting on it
 - Free from all other bodies in the actual situation





How to Construct a Free-Body Diagram

- 1. Decide which body (or combination of bodies) is to be isolated and analyzed (shown in the free-body diagram)
- 2. Draw a figure of the particle(s) isolated from its "environment"
- 3. Replace al physical contacts between the particle and the environment with forces (of assumed direction)
 - Contact forces occur from bodies, connections, friction in physical contact with the particle
 - Body forces is a force that acts throughout the volume of a body
 - i.e. the earth-pull on (or weight of) a body
- 4. Choose the set of coordinate axes to be used in solving the problem and indicate their directions on the free-body diagram.
 - Place any dimensions required for solution of the problem on the diagram.



Tips for Drawing a Correct FBD

- <u>Always</u> establish the x, y, and z axes
- <u>Always</u> draw your FBD first
- Label <u>ALL</u> known and unknown force magnitudes and directions on the diagram
- Label <u>ALL</u> dimensions
- **Calculate** important angles
- The sense of a force having an unknown magnitude can be assumed
 If the solution is negative, then the assumed direction is incorrect (opposite of what you assumed)

• A cable and spring are tied together at C and are loaded with a mass of 120 kg. Determine the tension in cable AC and the change in length (in mm) of the spring if the spring stiffness, k, is 1.35 kN/mm and the system is in equilibrium.









• Three cables are used to tether a balloon as shown. Knowing that the balloon exerts an 800 N vertical force at A, determine the tension in each wire.



