DRAG FORCE CALCULATION

"Drag is the component of force on a body acting parallel to the direction of relative motion." [1] This can occur between two differing fluids or between a fluid and a solid. In this lab, the drag force will be explored between a fluid, air, and a solid shape.

Drag force is a function of shape geometry, velocity of the moving fluid over a stationary shape, and the fluid properties density and viscosity. It can be calculated using the following equation,

$$F_D = \frac{1}{2} \rho A C_D V^2$$

Equation 1: Drag force equation using total profile

where

ρ is density determined from Table A.9 or A.10 in your textbook
A is the frontal area of the submerged object
C_D is the drag coefficient determined from Table 1
V is the free-stream velocity measured during the lab

Table 1: Known drag coefficients for various shapes

Body	Status	Shape	CD
Square Rod	Sharp Corner		2.2
Circular Rod		≡ O	0.3
Semicircular Rod	Concave Face	₽ŧ	1.2
	Flat Face	≡D	1.7

The drag force of an object can also be calculated by applying the conservation of momentum equation for your stationary object.

$$\vec{F} = \frac{\partial}{\partial t} \int_{CV} \vec{V} \,\rho d\,\forall + \int_{CS} \vec{V} \,\rho \vec{V} \cdot d\vec{A}$$

Assuming steady flow, the equation reduces to

$$\vec{F} = \int_{CS} \vec{V} \rho \vec{V} \cdot d\vec{A}$$

The following frontal view of the duct is shown below. Integrating the velocity profile after the shape will allow calculation of drag force per unit span.



Figure 1: Velocity profile after an inserted shape.

Combining the previous equation with Figure 1, the following equation is obtained:

$$D_f = \int_0^W \rho U_i (U_\infty - U_i) L dy$$

Simplifying the equation, you get:

$$D_f = \rho L \sum_{i=1}^{20} U_i (U_{\infty} - U_i) \Delta y$$

Equation 2: Drag force equation using wake profile

The pressure measurements can be converted into velocity using the Bernoulli's equation as follows:

$$U_i = \sqrt{\frac{2\Delta P_i}{\rho_{Air}}}$$

Be sure to remember that the manometers used are in W.C. which will require a substitution of ρ_{H20} gh for ΔP . Refer to page 1 of the lab procedures for Inside Wind Tunnel II for more information.

Experimental Setup:



Figure 2: Experimental Setup for Drag Calculation Lab

Procedure:

- 1. Turn off the fan & power if necessary.
- 2. Install the square rod into the straight duct with a slat as shown and set up in wind tunnel.
- 3. Zero manometer 5.
- 4. Connect the hoses to the appropriate manometer shown.
- 5. Insert the probe approximately 4" behind the object and set it on the bottom surface of the duct.
- 6. Set the fan to a setting of 80 and move the probe up in 1 cm steps taking readings at each of these points until the top of the duct is reached. <u>When taking the readings, it is important to not shake or bump the table as well as to not walk near the inlet or exit of the wind tunnel.</u>

- Use the attached anemometer in the upper left-hand corner of the wind tunnel to measure the free-stream velocity 2" from the top of the duct at the beginning of the slat.
- 8. Repeat steps 2-7 for each rod shape and orientation designated in Table 2.

	Square Rod	Circular Rod	Semicircular Bod: Concave	Semicircular Rod: Elat Face
Position (cm)	ΔP (in _{H2O})	ΔP (in _{H20})	ΔP (in _{H20})	$\Delta P (in_{H2O})$
1	((
2				
3				
4				
5				
6				
7				
8				
9				
10				
11				
12				
13				
14				
15				
16				
17				
18				
19				
20				
Velocity (ft/s)				
Frontal Area				
(ft ²)				

Table 2: Pressure, velocity, and area data for different shaped rods

LAB NOTEBOOK:

- Using Equation 1, calculate the drag force for each rod shape.
- Using Equation 2, calculate the drag force for each rod shape.
- Compare the calculated drag force for each rod shape using both equations.
- Graph the velocity profile for each rod shape.