

# The Roomba coverage problem

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- ▶ **Empty Room**

- ▶ Observation: you already know how to get to a corner and how to cover rows or columns

- ▶ **Step-by-step Decomposition**

- ▶ (Each step is one or more states)
- ▶ Go to the top left corner
- ▶ Paint the top row going East
- ▶ Move down one
- ▶ Paint the next row going West
- ▶ Move down one
- ▶ Repeat



# The Roomba coverage problem

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- ▶ **Step-by-step Decomposition**

- ▶ Go to the top left corner

- 0 X\*\*\* -> N 0

- 0 N\*\*\* -> X 1

- 1 \*\*X\* -> W 1

- 1 \*\*W\* -> X 2

- ▶ Paint the top row going East

- 2 \*X\*\* -> E 2

- 2 \*E\*\* -> X 3

- ▶ Move down one

- 3 \*\*\*\* -> S 4

- ▶ Paint the next row going West

- 4 \*\*X\* -> W 4

- 4 \*\*W\* -> X 5

- ▶ Move down one, and repeat from 2

- 5 \*\*\*\* -> S 2



# Simplify!

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## ▶ Step-by-step Decomposition

### ▶ Go to the top left corner

0 X\*\*\* -> N 0

0 N\*\*\* -> X 1

1 \*\*X\* -> W 1

1 \*\*W\* -> X 2

### ▶ Paint the top row going East

2 \*X\*\* -> E 2

2 \*E\*\* -> X 3

### ▶ Move down one

3 \*\*\*\* -> S 4

### ▶ Paint the next row going West

4 \*\*X\* -> W 4

4 \*\*W\* -> X 5

### ▶ Move down one, and repeat from 2

5 \*\*\*\* -> S 2

## ▶ Simplified by combining rules

### ▶ Go to the top left corner

0 X\*\*\* -> N 0

0 N\*X\* -> W 0

0 N\*W\* -> X 1

### ▶ Paint the top row going East, *and move down one*

1 \*X\*\* -> E 1

1 \*E\*\* -> S 2

### ▶ Paint the next row going West, *and move down one*

2 \*\*X\* -> W 2

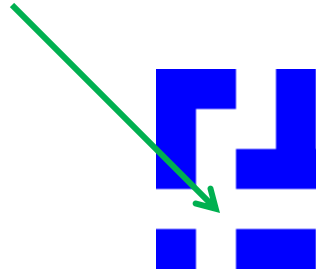
2 \*\*W\* -> S 1



# The maze coverage problem

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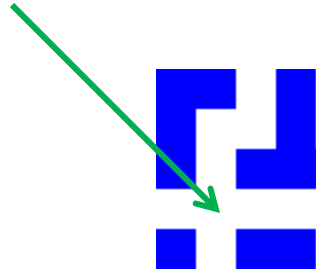
- ▶ Keep your right hand on a wall at all times
- ▶ Strategy: start considering possible *cases* or *scenarios*
- ▶ If you are here, which way do you go?



# The maze coverage problem

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- ▶ Keep your right hand on a wall at all times
- ▶ Strategy: start considering possible *cases* or *scenarios*
- ▶ If you are here, which way do you go?



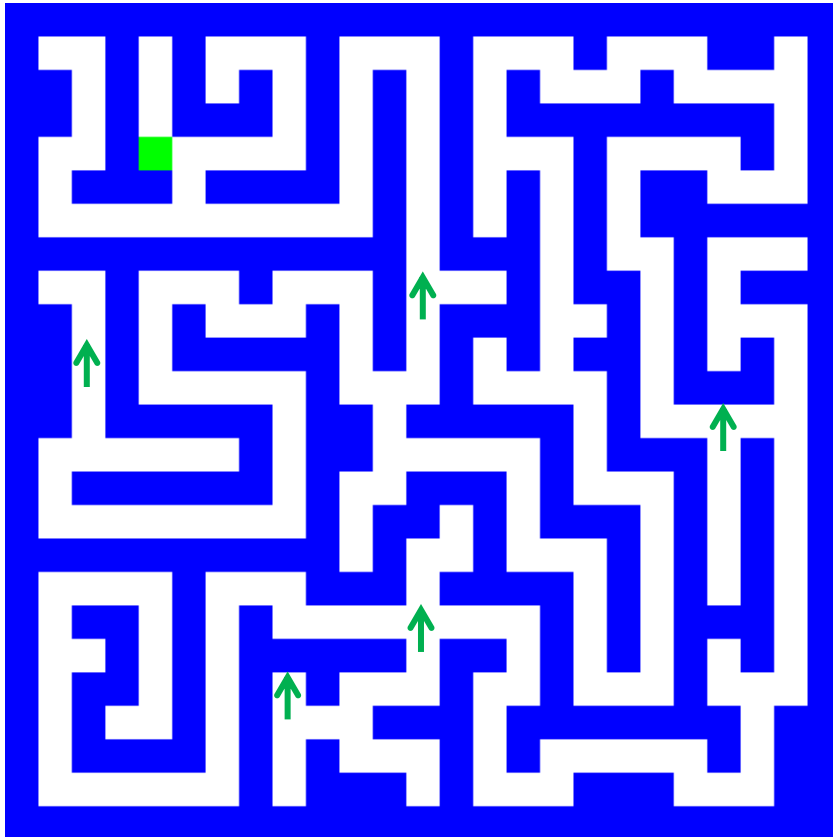
- ▶ Answer: depends on which way you are *facing*
  - ▶ The environment is XXXX (no blocking) no matter what
  - ▶ So use state to represent differences in facing!



# The maze coverage problem

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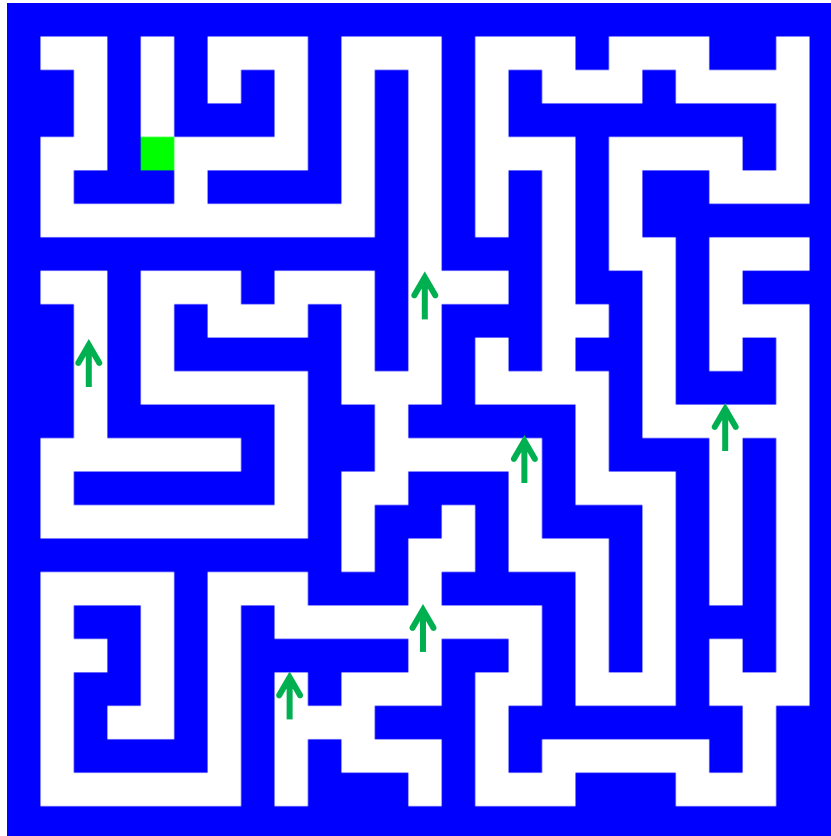
- ▶ Keep your right hand on a wall at all times



# The maze coverage problem

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- ▶ Keep your right hand on a wall at all times



Open to the right, turn right

Blocked right, move forward

Blocked right and forward, turn left

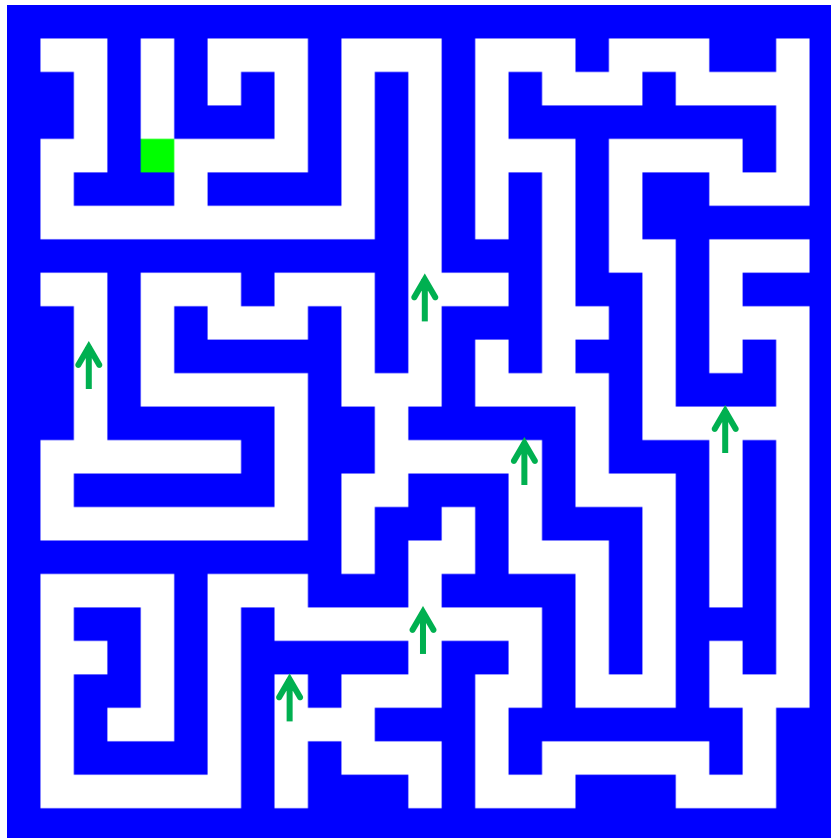
Blocked right, forward and left, turn back



# The maze coverage problem

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- ▶ Keep your right hand on a wall at all times



State 0 is facing N, 1 is E, 2 is S and 3 is W

Open to the right, turn right

0 \*x\*\* -> E 1

Blocked right, move forward

0 xE\*\* -> N 0

Blocked right and forward, turn left

0 NEx\* -> W 3

Blocked right, forward and left, turn back

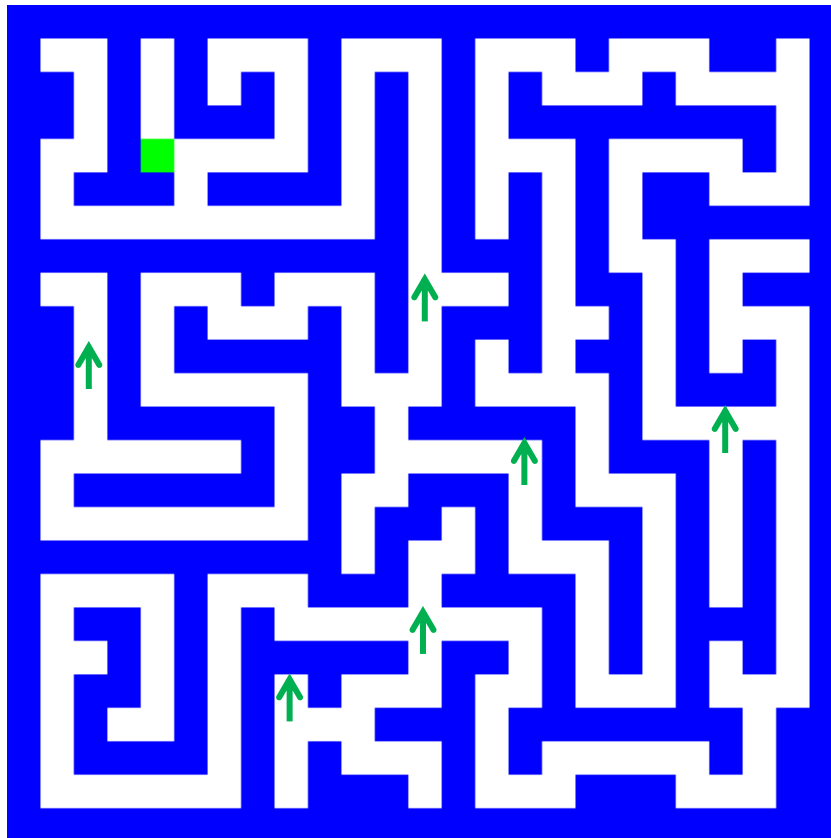
0 NEW\* -> S 2





# The maze coverage problem

- ▶ Keep your right hand on a wall at all times



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0 *x** -> E 1
0 xE** -> N 0
0 NEx* -> W 3
0 NEW* -> S 2

1 ***x -> S 2
1 *x*S -> E 1
1 xE*S -> N 0
1 NE*S -> W 3

2 **x* -> W 3
2 **Wx -> S 2
2 *xWS -> E 1
2 *EWS -> N 0

3 x*** -> N 0
3 N*x* -> W 3
3 N*Wx -> S 2
3 N*WS -> E 1
```

Surely this can  
be simplified!  
(the creator's record is  
8 rules)

