Energy estimates for Klein-Gordon type equations with time dependent mass

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We consider the energy estimate of the solution to the Cauchy problem of Klein-Gordon type equation with time dependent mass:

$$\begin{cases} \partial_t^2 u - \Delta u + M(t)u = 0, & (t,x) \in (0,\infty) \times \mathbb{R}^n, \\ u(0,x) = u_0(x), \quad \partial_t u(0,x) = u_1(x), & x \in \mathbb{R}^n, \end{cases}$$

where $M(t)$ is real valued, oscillating and not necessarily positive. The main purpose of my talk is to give sufficient conditions to $M(t)$ for the energy to be asymptotically stable.